



**CS649**

**Sensor Networks**

**IP Track Lecture 3: Distributed Target Tracking in  
Sensor Networks**

I-Jeng Wang

<http://hinrg.cs.jhu.edu/wsn06/>

# Multiple Target Tracking in Wireless Sensor Networks

- Problem: Based on distributed sensor measurements, sensor nodes collaborate to detect presence of targets of interests, estimate and update (track) states (position, velocity, etc.) of targets over time.
- Key Challenges:
  - Data/information dissemination, management, and storage
  - Dynamic resource allocation and control
  - Combining measurements from multiple and potentially multimodal sensors (data fusion problem)
  - Multiple target disambiguation
  - Operating under uncertainty
  - Real-time constraints

# Traditional (Centralized) Multiple Target Tracking (MTT) Problem

- Measurements (radar returns, acoustic detections, etc.) arrives over time and are typically processed at a centralized location
- Two Key Sub-Problems
  - **Data association**: find a partition of observations such that each element of a partition is a collection of observations generated by a single target or clutter
  - **State estimation**: incrementally estimate and update the state (position) of each target over time
  - Two problems are intertwined
- Other Important Issues
  - Track initiation and management
  - Target identification and classification

# Basic Formulation of Bayesian Tracking for a Single Target\*

- State transition model

$$\mathbf{x}_k = \mathbf{f}_k(\mathbf{x}_{k-1}, \mathbf{v}_{k-1})$$

i.i.d. process noise

- Measurement model

$$\mathbf{z}_k = \mathbf{h}_k(\mathbf{x}_k, \mathbf{n}_k)$$

i.i.d. measurement noise

- Bayesian filter (tracker)

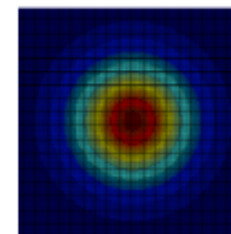
**Belief update** 
$$p(\mathbf{x}_k | \mathbf{z}_{1:k}) = \frac{p(\mathbf{z}_k | \mathbf{x}_k) p(\mathbf{x}_k | \mathbf{z}_{1:k-1})}{p(\mathbf{z}_k | \mathbf{z}_{1:k-1})}$$

**Prediction** 
$$p(\mathbf{x}_k | \mathbf{z}_{1:k-1}) = \int p(\mathbf{x}_k | \mathbf{x}_{k-1}) p(\mathbf{x}_{k-1} | \mathbf{z}_{1:k-1}) d\mathbf{x}_{k-1}$$

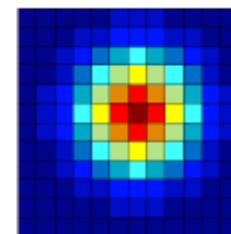
**Normalization** 
$$p(\mathbf{z}_k | \mathbf{z}_{1:k-1}) = \int p(\mathbf{z}_k | \mathbf{x}_k) p(\mathbf{x}_k | \mathbf{z}_{1:k-1}) d\mathbf{x}_k$$

# Specific Bayesian Tracking Algorithms

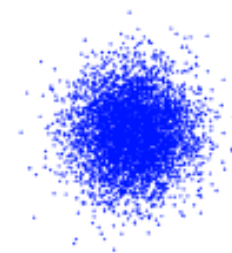
- Kalman Filter
  - Linear state transition and measurement models
  - Gaussian process and measurement noises
  - Bayesian filter reduces to sequential updates of mean and covariance matrix of the state
  - Extended Kalman filter for nonlinear cases via linearization
- Grid-Based Methods
  - Discrete state space (or discretize the state space as an approximation)
  - Update posterior probability at the discrete states
- Particle Filtering Methods
  - Approximate the brief function by randomly sample the state space using sequential Monte Carlo techniques



Gaussian  
(Parametric)



Grid



Particles

# Traditional Data Association Approaches for MTT

- Nearest neighbor (possibly with assignment algorithms)
  - Associate with each track the measurement closest to its prediction (either Euclidean or Mahalanobis distance)
- Multiple Hypothesis Tracker (MHT)
  - Simultaneously maintain multiple hypotheses of association that has high scores
  - Dynamically prune or discard hypotheses to avoid explosion of number of hypotheses
- Joint Probability Data Association (JPDA)
  - Associate all measurements with high prediction scores to each track
  - Update the belief with all measurements
- Comparisons and Implementation Issues for Sensor Networks



# Information-Driven Dynamic Sensor Collaboration for Tracking Applications

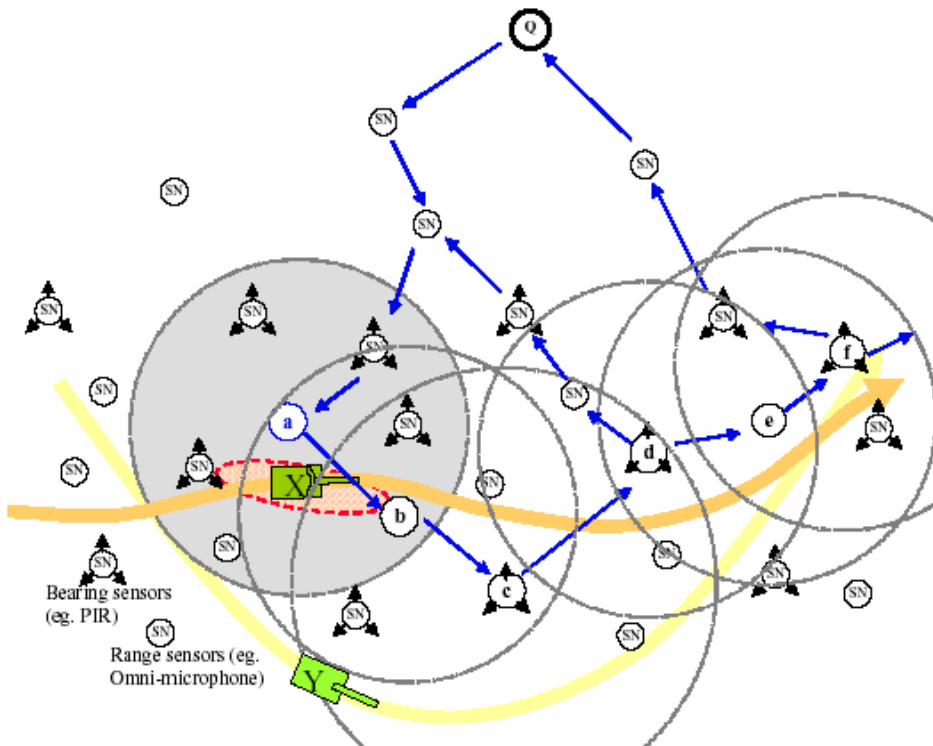
Feng Zhao

Jaewon Shin

James Reich

*IEEE Signal Processing Magazine, 2002*

# A Tracking Scenario

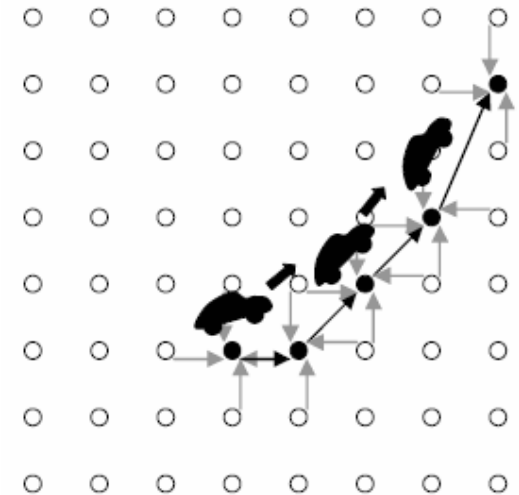


- *Discovery*: Node *a* detects *X* and initializes tracking
- *Query Processing*: A query is routed toward region of interest (around *a*)
- *Collaborative Processing*: Node *a* collaborate with other nodes to estimate the target states
- *Communication*: *a* hands off estimate to *b*, *b* to *c*, etc.
- *Reporting*: Node *d* or *f* reports tracking information back to the querying node
- *Data Association* if multiple targets

# Basic Setting and the Leader-Based Approach (Single Target)

$$\underbrace{p(\mathbf{x}^{(t+1)} | \overline{\mathbf{z}^{(t+1)}})}_{\text{updated belief}} \propto \underbrace{p(\mathbf{z}^{(t+1)} | \mathbf{x}^{(t+1)})}_{\text{new data}} \cdot \int p(\mathbf{x}^{(t+1)} | \mathbf{x}^{(t)}) \underbrace{p(\mathbf{x}^{(t)} | \overline{\mathbf{z}^{(t)}})}_{\text{current belief}} d\mathbf{x}^{(t)}$$

- At any time instant, there is only one leader where
  - A new measurement is taken
  - Belief is updated based on Bayesian filtering
- The leader selects the new leader node from its neighborhood to handoff the tracking responsibility
  - Communicate the current belief to the new leader
- Minimize communication of measurements across nodes



# Information-Directed Approach for Leader Selection

- Basic idea: Select sensors to collaborate (and the leader node for handoff) based on information utility measures and appropriate cost function (e.g. communications, energy)

measurements including data from node  $j$

measurement from node  $j$

$$O(p(\mathbf{x} | \overline{\mathbf{z}}_j^{(t)})) = \alpha \phi(p(\mathbf{x} | \overline{\mathbf{z}}_{j-1}^{(t)}, \mathbf{z}_j^{(t)})) - (1 - \alpha) \psi(\mathbf{z}_j^{(t)})$$

Overall value by incorporating measurement from node  $j$

Information utility of measurement from node  $j$  (e.g. mutual information)

Cost of incorporating measurement from node  $j$

$$\hat{j} = \arg \max_{j \in A} O(p(\mathbf{x} | \{\mathbf{z}_i\}_{i \in U} \cup \{\mathbf{z}_j\}))$$

# Metrics for Information Utility

- Information-theoretic measure: Entropy

$$\varphi(p(\mathbf{x} | \{\mathbf{z}_i\}_{i \in U} \cup \{\mathbf{z}_j\})) \triangleq -H_p(x). \quad H_p(x) = - \int_S p(x) \log p(x) dx$$

- Mahalanobis distance measure

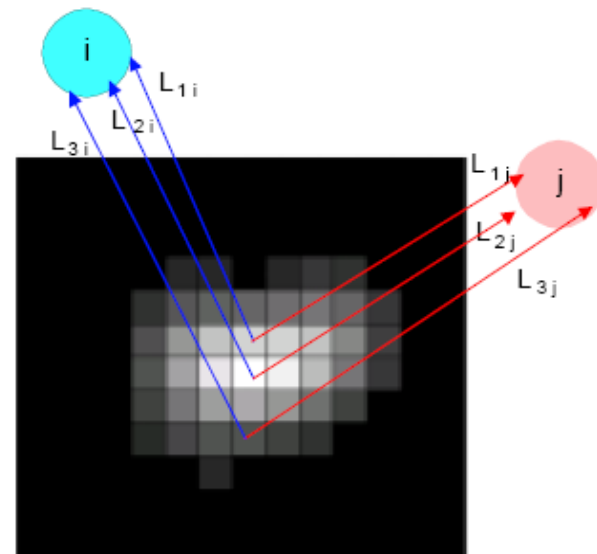
$$\varphi(\mathbf{x}_j, \hat{\mathbf{x}}, \hat{\Sigma}) = -(\mathbf{x}_j - \hat{\mathbf{x}})^T \hat{\Sigma}^{-1} (\mathbf{x}_j - \hat{\mathbf{x}})$$

- Expected posterior distribution

$$\hat{p}(\mathbf{x}^{(t+1)} | \overline{\mathbf{z}^{(t+1)}}) = C \cdot \hat{p}(\mathbf{z}_i^{(t+1)} | \mathbf{x}^{(t+1)}) \cdot p(\mathbf{x}^{(t+1)} | \overline{\mathbf{z}^{(t)}})$$

$$\hat{p}(\mathbf{z}_i^{(t+1)} | \mathbf{x}^{(t+1)}) = \sum_{v_k \in S(\mathbf{x}^{(t+1)})} L_{ki}(\mathbf{x}^{(t+1)}, v_k) \cdot \left[ p(\mathbf{x}^{(t+1)} | \overline{\mathbf{z}^{(t)}}) \Big|_{\mathbf{x}^{(t+1)}=v_k} \right]$$

$$L_{ki}(\mathbf{x}^{(t+1)}, v_k) \triangleq \hat{p}(\mathbf{z}_i^{(t+1)} | \mathbf{x}^{(t+1)} = v_k)$$



# Pros and Cons of the Simple Leader-Based Approach

- Pros:
  - Minimizes communications of measurements
  - Good scalability with number of targets (only one active node for each target) if targets are well separated
  - Appropriate for network of low-power devices
- Cons:
  - Potential issue with many redundant tracks without proper track initiation and management
  - Difficulties in handling ambiguity with track collisions resulting from redundant tracks or target crossovers
  - Minimum use of collaborative signal processing to improve localization and tracking performance



# Distributed Group Management for Track Initiation and Maintenance in Target Localization Applications

Juan Liu

Jie Liu

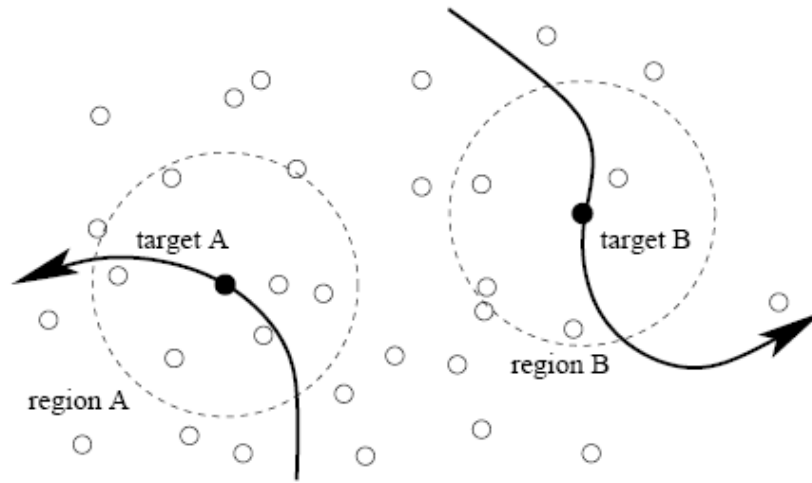
James Reich

Patrick Cheung

Feng Zhao

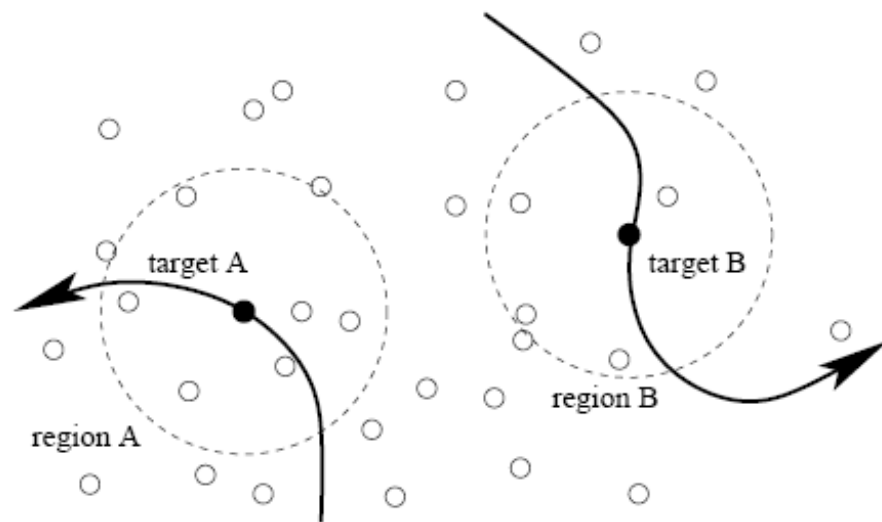
*IPSN, 2003*

# Geographically Based Group Management



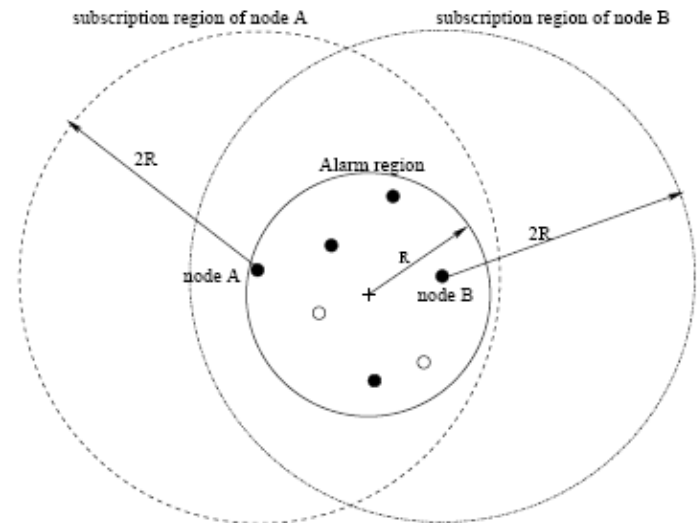
# Geographically Based Group Management

- Dynamically form and maintain collaborative groups based on proximity
- At any point of time, each group has a unique leader and focuses on tracking a target using the leader-based tracking technique
- Information dissemination is constrained to each group using geographical-based routing protocols



# Distributed Detection and Track Initiation

- Each node runs a stand-alone detection using the likelihood ratio detector
- Nodes with detection form a collaborative group and elect a leader by
  - Broadcast its detection (with detection time and score) to neighbors within  $2R$  radius
  - Among all detect received within  $t_{comm}$  select an leader with earliest timestamp (or highest likelihood ratio if tied)
- The leader suppresses all nodes within radius  $2R$  from further detection to prevent creation of redundant track
- The leader initializes the belief state and starts the tracking algorithm



# Dynamic Group Maintenance Via Suppression and Unsuppression

- As the leader handoffs its responsibility to a new leader based on the information-based method, the leader use SUPPRESSION and UNSUPPRESSION messages to update the group membership and prevent new detections of the same target from initiating redundant track
- The suppression region is determined based on the current belief state

